

Simple Harmonic Motion: PIETER'S GROUP

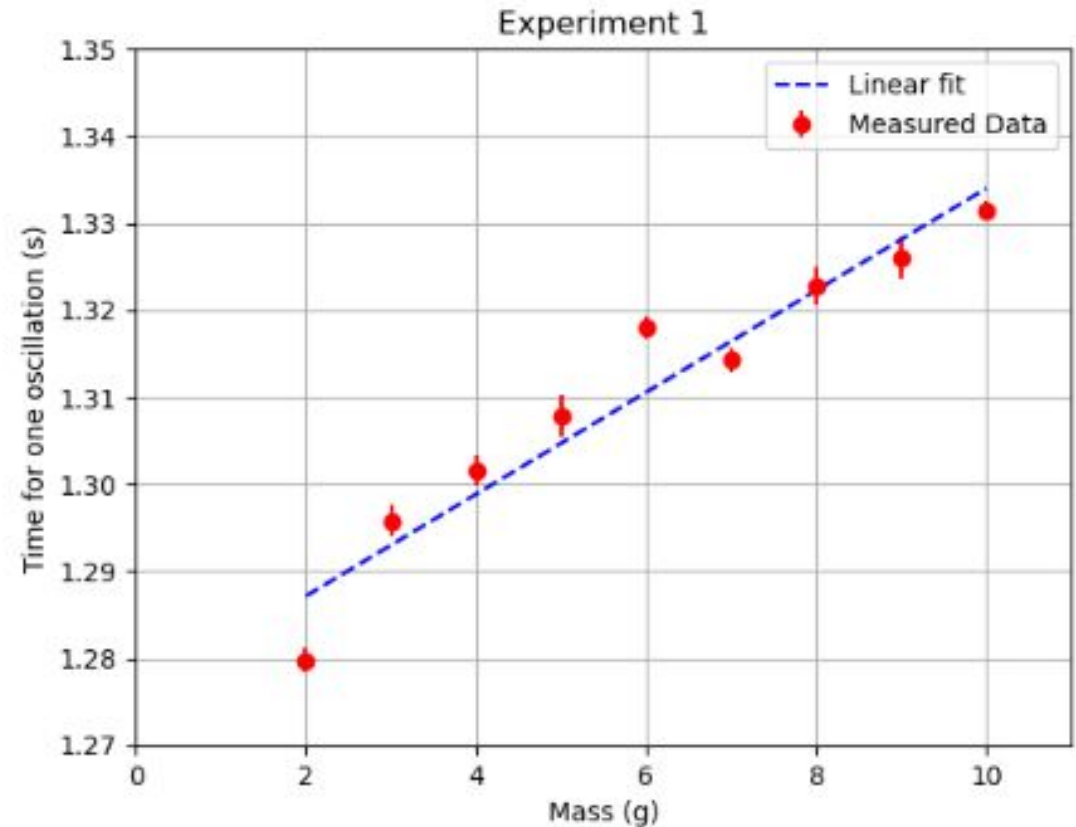
Jack, Jonas, Hansun, Winnie, Thomas, Bryce, Altar

Table of Contents

- Experiment 1 : Methodology & Data
- Experiment 2 : Methodology
- Experiment 2 : Data
- Experiment 3 : Method 1
- Experiment 3 : Method 2
- Experiment 3 : Fourier Transform
- Simulation 1
- Simulation 2

Experiment 1 Methodology & Data

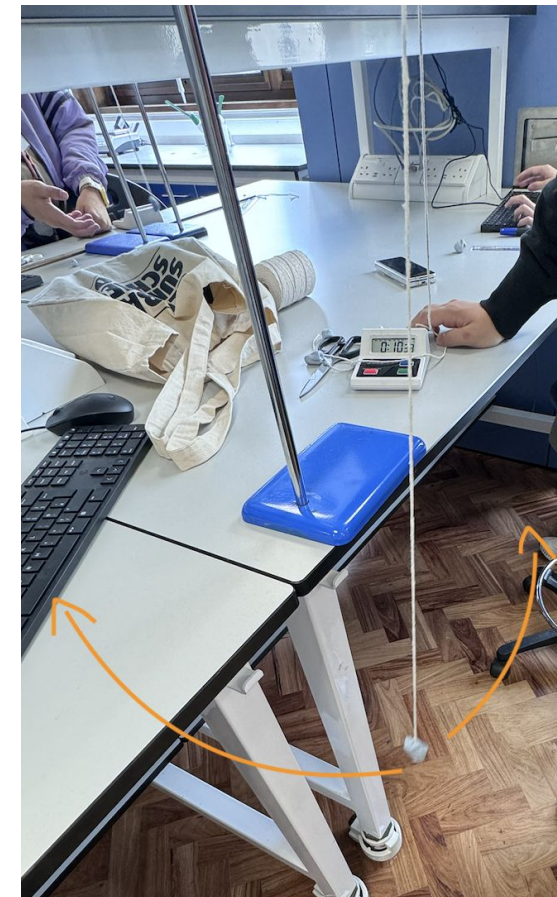
- Linear fit $T = m \cdot a + b$
 - $a = 0.006 \pm 0.001$
 - $b = 1.275 \pm 0.004$
- Small gradient a , confirming hypothesis of no mass dependence
- Slight upward trend due to moving centre of mass and friction



Experiment 2 Methodology

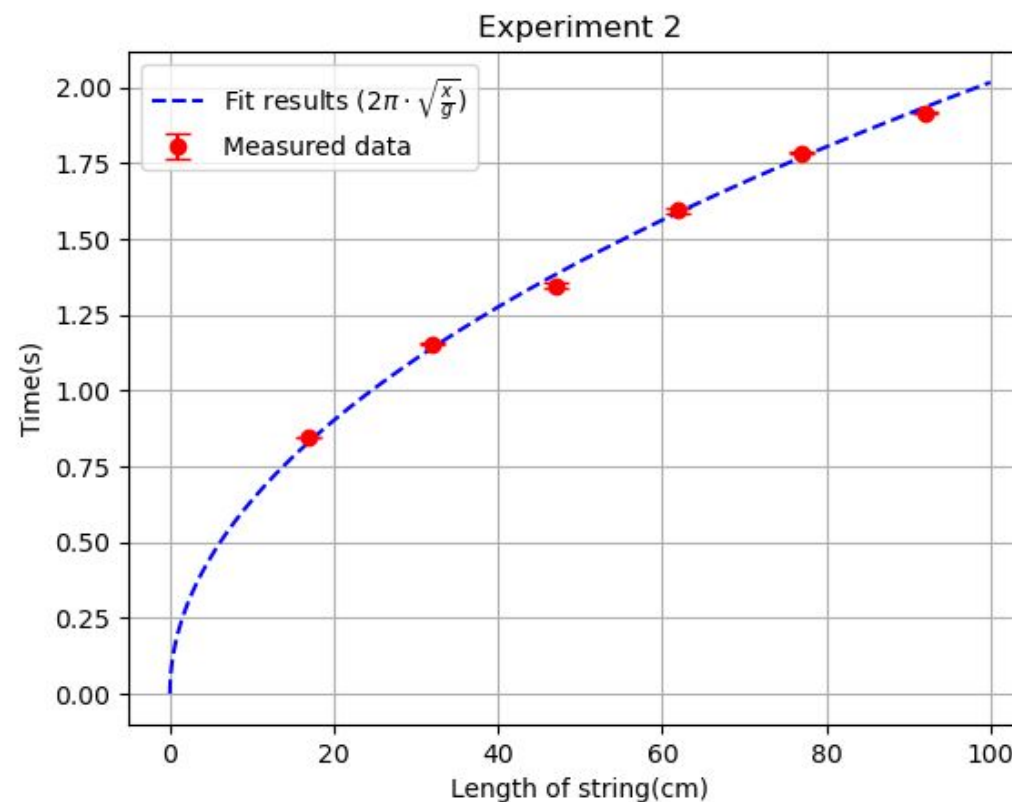
How we took the data(setup):

- Setup:
 1. Centre Of Mass is ensured by making a round ball
 - *2. Ball hanged off the table to allow for greater string lengths
 - *3. Make sure to include the distance from the top of the ball to the Centre Of Mass
- Reducing uncertainty:
 1. Record TEN oscillations and divide to get time of one oscillation
 2. Repeat five trials at every length of the string and take AVERAGE



Experiment 2 Data

- Error bars
 - Calculated the standard deviation across the 5 trials
 - Divided the standard deviation by the $\sqrt{5}$ for error on mean
- $g = 9.70 \pm 0.09 \text{ ms}^{-2}$
- Reasons for discrepancy
 - Friction
 - Center of mass

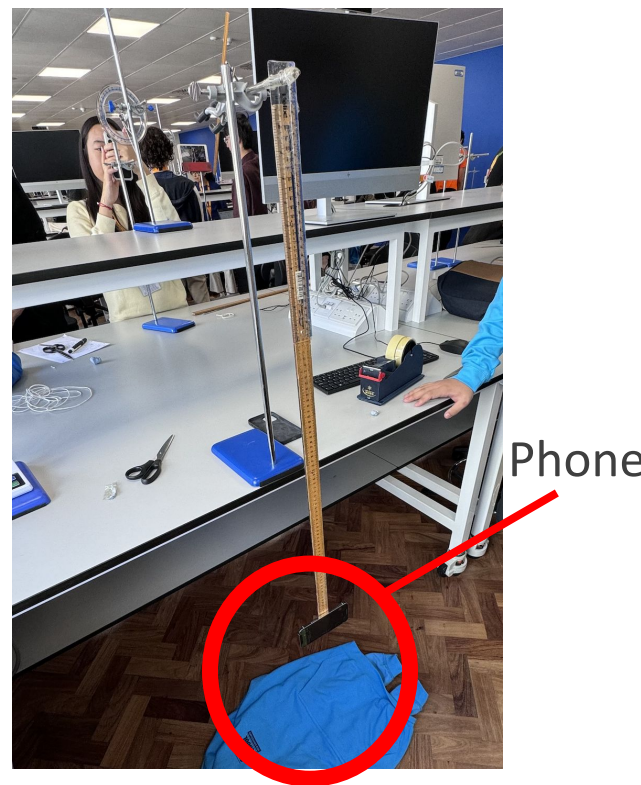


EXPERIMENT 3 SETUP

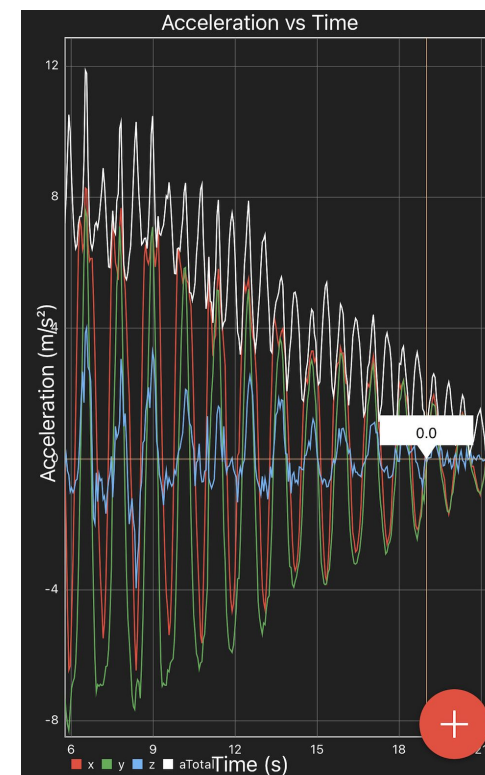
Method 1



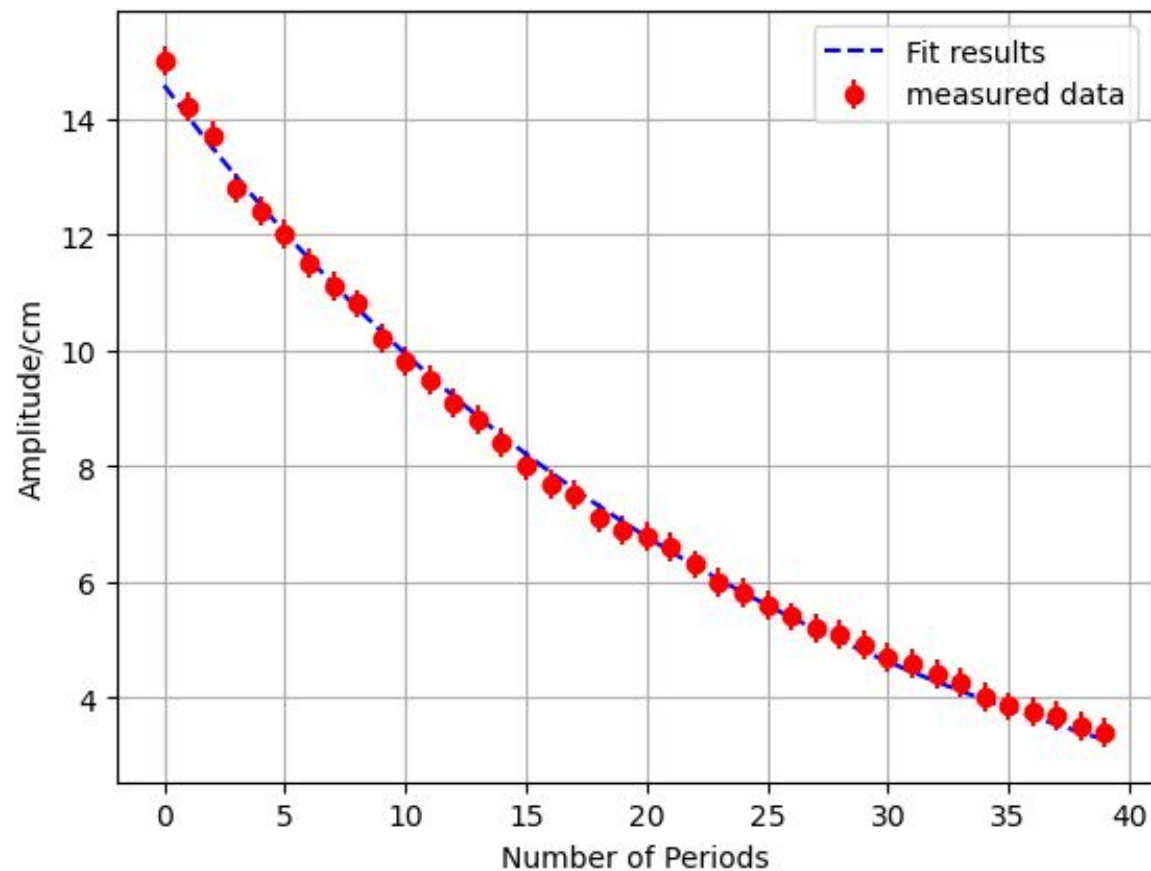
Method 2



Data of method 2



Experiment 3 Method 1



$$f(x) = a \cdot e^{-b \cdot x} \cdot \cos(\omega x + \phi)$$

$$f(x) = a \cdot e^{-b \cdot x}$$

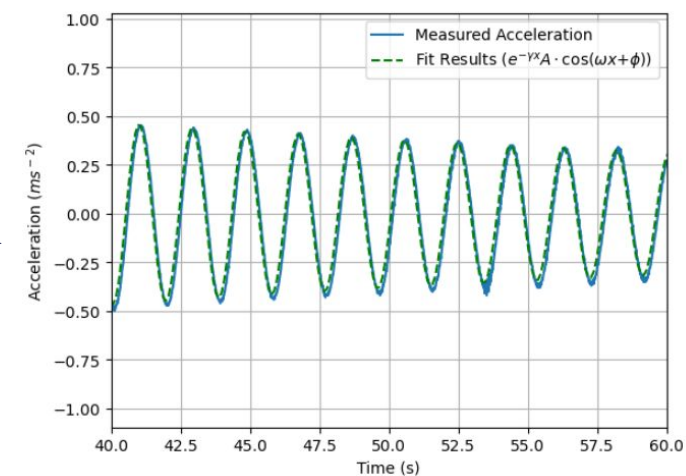
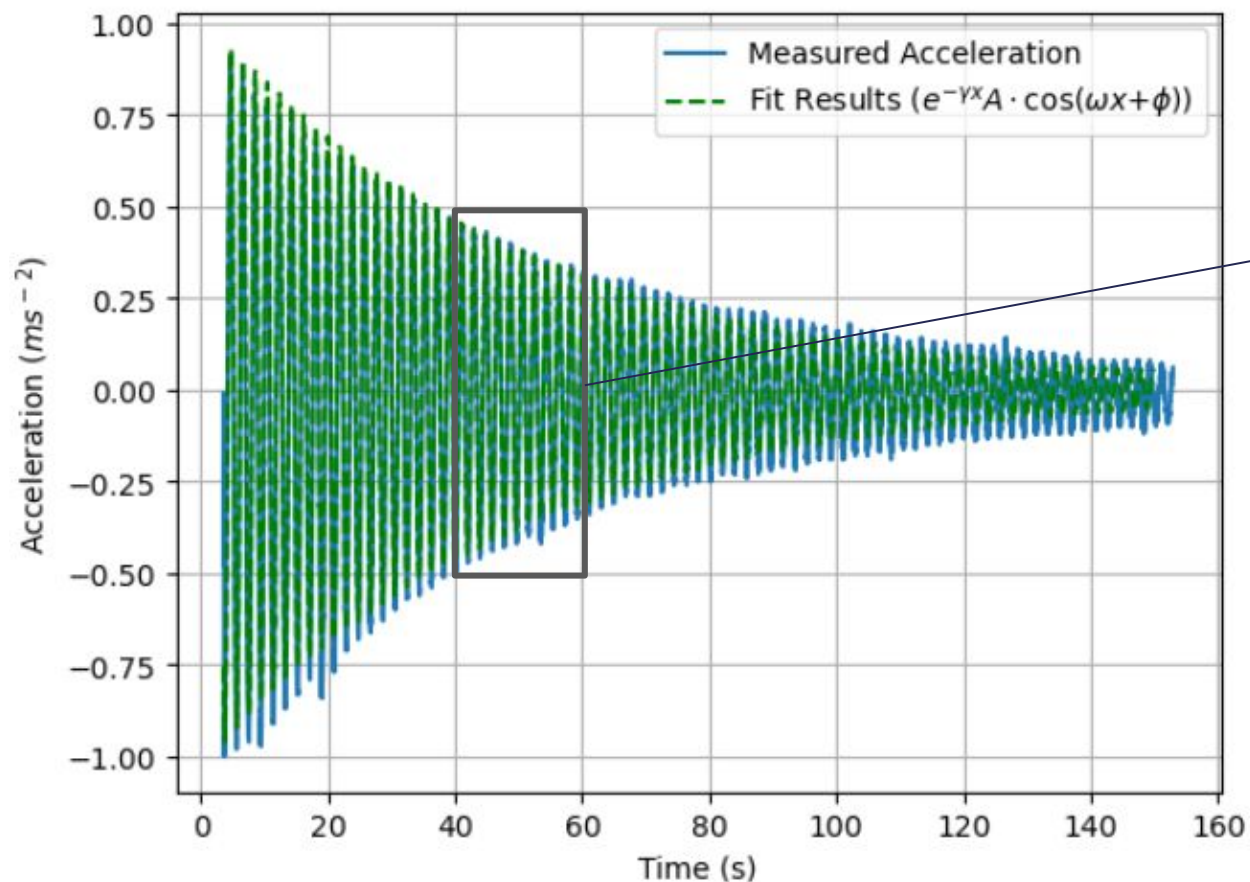
So the values with errors are:

$$a = 14.57 \pm 0.06 \text{ cm}$$

$$b = 0.0383 \pm 0.0003$$

**Indicates the trend of
exponential decay.**

Experiment 3 Method 2



$$\omega = 3.2904 \pm 0.00008 \text{ s}^{-1}$$

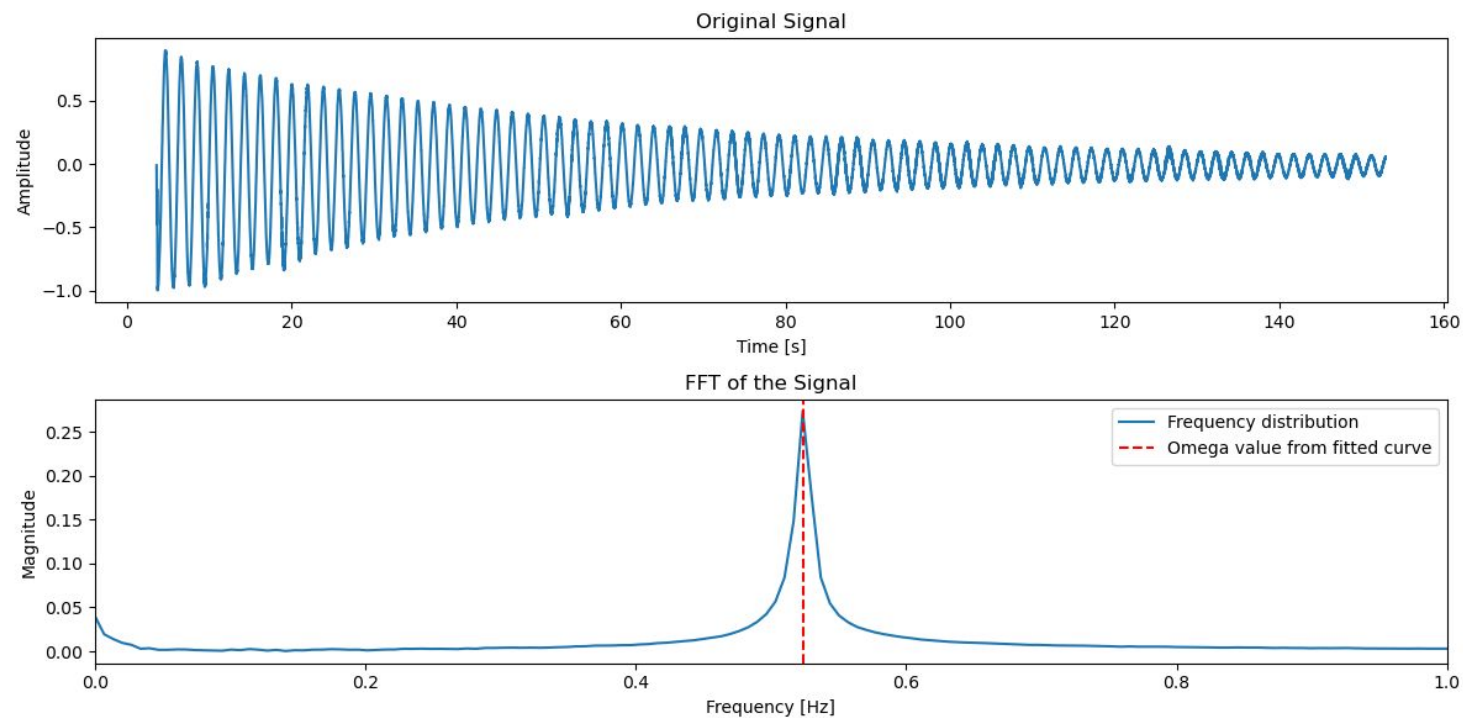
$$A = 1.032 \pm 0.003 \text{ s}^{-2}$$

$$\phi = -1.44 \pm 0.003 \text{ rad}$$

$$\gamma = 0.01986 \pm 0.00008 \text{ s}^{-1}$$

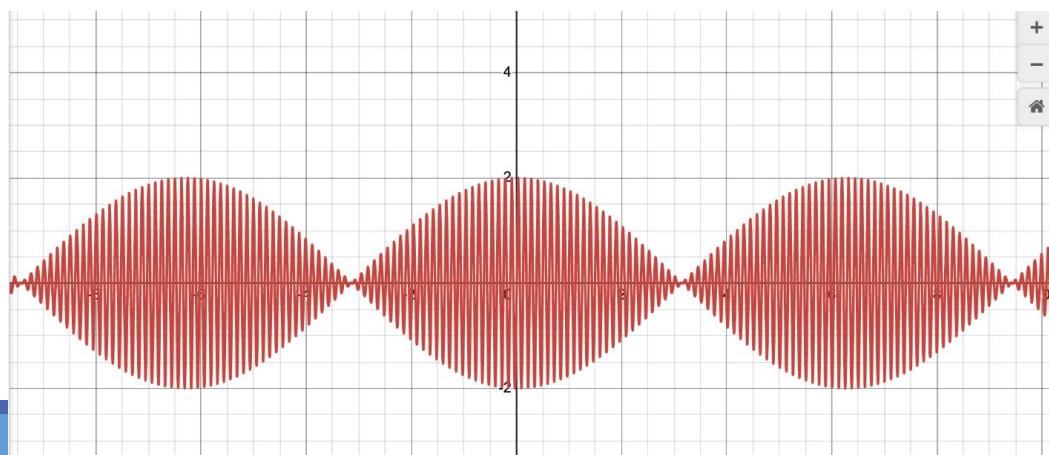
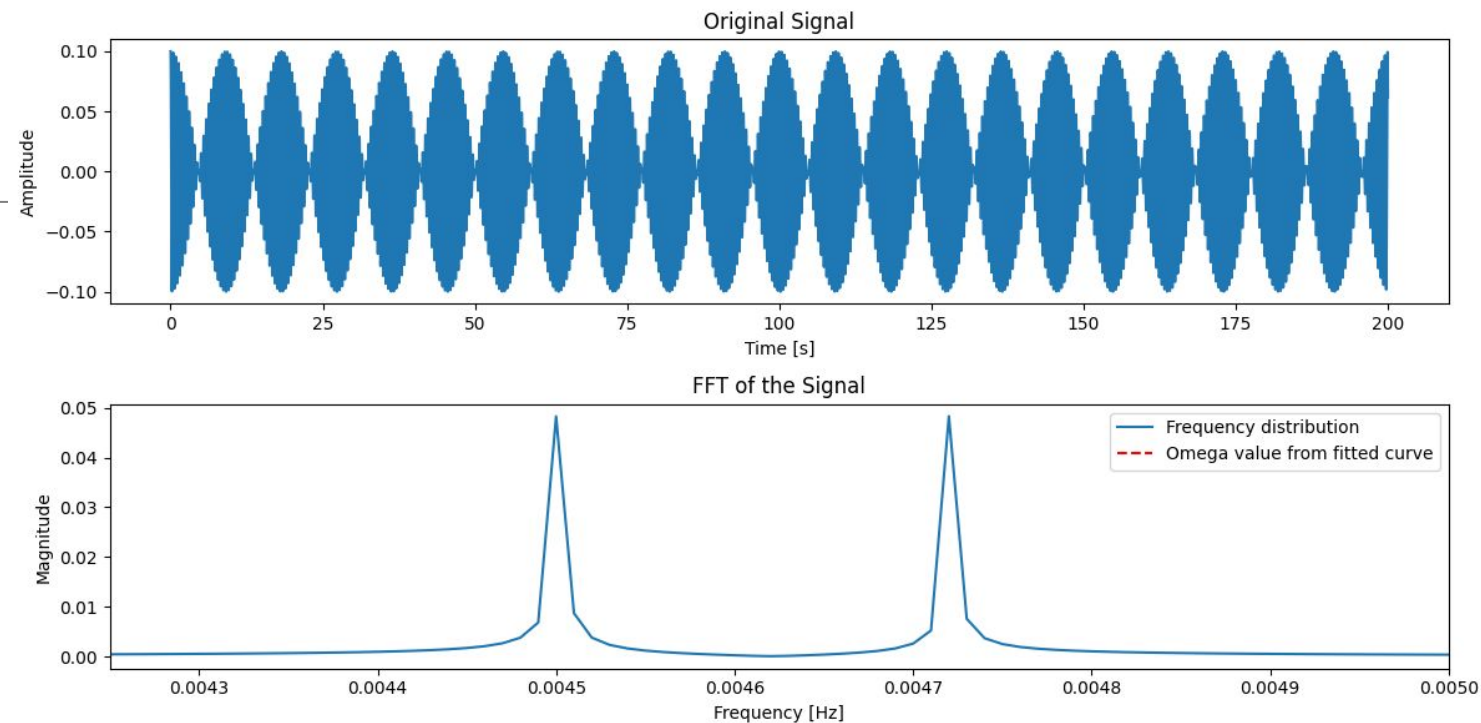
Experiment 3 Fourier Transform

- Fourier Transform of measured data.
- Peak at $F = 3.2904/2\pi \text{ s}^{-1}$
- Matches ω value from curve fit
- Width of peak determined by decay



Simulation 1

- Fourier Transform of coupled oscillators
- Expected sum of 2 Sinusoidal functions
- Transform confirms
- Confirmed 2 sinusoidal waves with similar frequencies
- Mean is the smaller frequency
- Difference is larger frequency

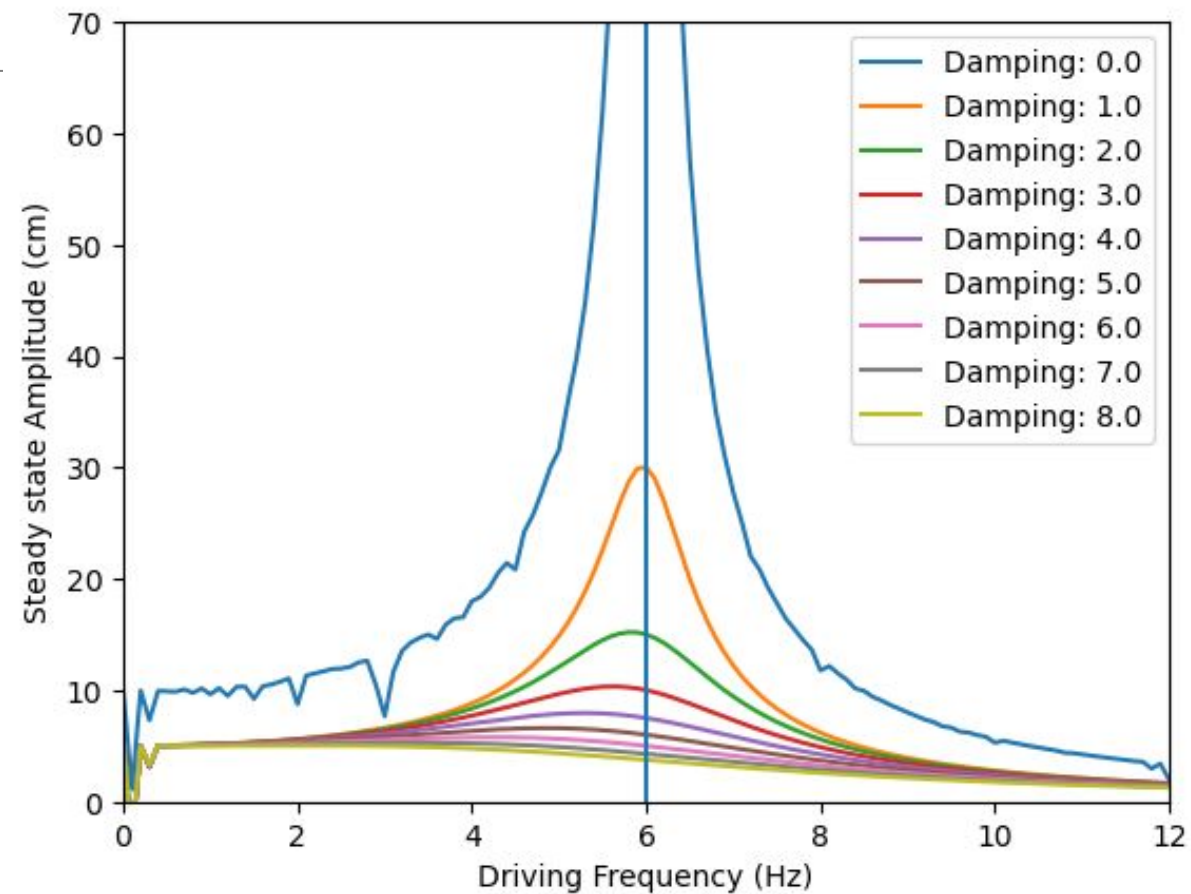


$\sin(50x) + \sin(51x)$
(on desmos)



Simulation 2

- Steady states amplitude from ODE solver
- Changing frequency from driver/piston
- Large resonance at and around natural frequency
- Resonance peak moves down, left and becomes broader with larger damping
- Damping coefficients are in Nsm^{-1}



Thanks for listening, any questions?